

# TRANSPORTNI UREĐAJI

## VJEŽBE - 13

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# INFORMACIJE

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-**POSLJEDNJE VJEŽBE !!!!**

-Za sve informacije – mail, konzultacije

-**2. KOLOKVIJ**

- 01.06.2011. – 12:00 – B dvorana

- **ANKETA !!!!!**



# ZADATAK 28 (1)

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Za pogonski mehanizam lifta prema slici zadano je:

nosivost  $m = 450$  kg; masa kabine  $m_{\text{kab}} = 700$  kg;

masa utega  $m_{\text{ut}} = 925$  kg;

$D = 550$  mm ( $D/d \geq 50$ );  $D_1 = 360$  mm ( $D_1/d \geq 35$ );

$h = 37,5$  m (visina dizanja);  $l_{\text{už}} = 40$  m (najveća viseća dužina užeta);

$\alpha = (8/9)\pi$ ;  $\gamma = (2/9)\pi$  (trapezni utor užnice);

$\eta_{\text{red}} = 0,65$  (pužni reduktor);  $\eta_0 = 0,98$  (užnica);

gubici vođenja kabine su (2 do 5) %, odabrano  $\eta_{\text{kab}} = 0,96$ ;

gubici vođenja utega su (1 do 3) %, odabrano  $\eta_{\text{ut}} = 0,98$ .

Elektromotor: "RK" 5ALV 160 MA-4/16; kW,  $M_n = 56$  Nm;  $M_p \approx 2,3M_n$ ;

$\omega_{\text{EM}} = 142,8$  s<sup>-1</sup>;  $I_{\text{EM}} = 0,115$  kgm<sup>2</sup>; s prisilnim hlađenjem, 180

ukapčanja/h.

Reduktor: "RK" W - 160,  $i_{\text{red}} = 36$ . Spojka s bubnjem kočnice: IS = 0,2 kgm<sup>2</sup>.

Čelično uže: Uže 10 DIN 3062 - FE - bk 1570 sZ, lift ima 4 užeta.

Značajke užeta:  $d = 10$  , Seal 8×(1+9+9);

računska lomna sila  $F_L = 537d^2$ , N ( $d$ , mm);  $q_m = 0,00348d^2$  kg/m ( $d$ , mm). Sigurnost užeta:  $S \geq 14$ .


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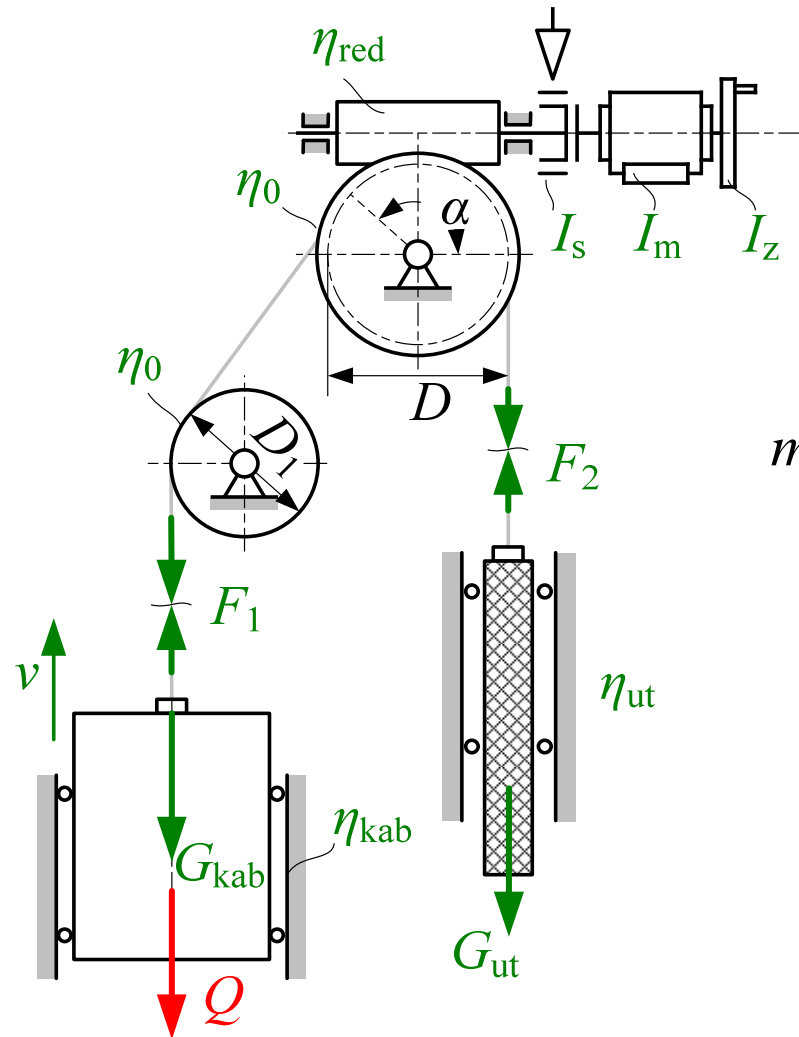
## ZADATAK 28 (2)

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Potrebno je provesti kontrolni proračun elemenata pogonskog mehanizma te kinematičkih i dinamičkih značajki sustava:

- provjeriti dimenzioniranje utega, užeta i motora;
  - izračunati brzinu dizanja s ugrađenim komponentama;
  - izračunati potrebni moment inercije zamašnjaka  $I_z$  tako da usporenje pri kočenju pune kabine prema gore ne premaši  $0,75 \text{ m/s}^2$ ;
  - izračunati vrijeme pokretanja pune kabine prema gore (s najniže postaje) i vrijeme kočenja pune kabine prema dolje (pred najnižom postajom);
  - provjeriti sigurnost protiv proklizavanja vučnog pogona pri ustaljenoj vožnji s punom i praznom kabinom te pri pokretanju i kočenju s punom kabinom;
  - izračunati granično usporenje pri kočenju s punom kabinom prema dolje kod kojeg bi sigurnost protiv proklizavanja bila jednaka 1.
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# ZADATAK 28 (3)



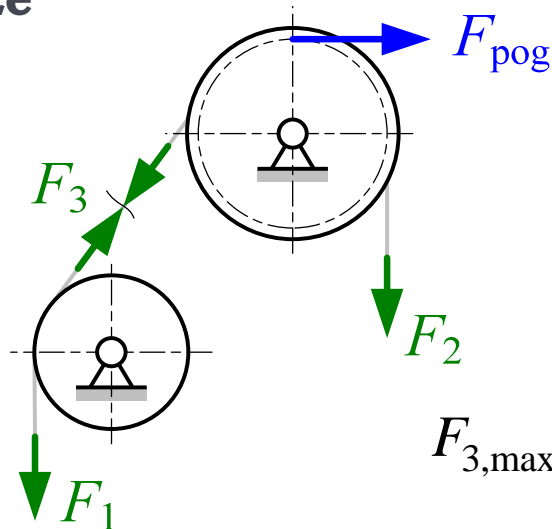
**Masa utega**

$$m_{ut} = m_{kab} + m / 2 = 700 + 450 / 2 = 925 \text{ kg}$$

Masa utega je dobro izabrana

# ZADATAK 28 (4)

Uže



$$F_{3,\max} = \frac{F_1}{\eta_0} = \left( \frac{Q + G_{\text{kab}}}{\eta_{\text{kab}}} + G_{\text{už}} \right) \frac{1}{\eta_0}$$

$$F_{3,\max} = \left( \frac{4414,5 + 6867}{0,96} + 546,2 \right) \frac{1}{0,98} = 12548,8 \text{ N}$$

Maksimalna statička sila u jednom užetu (kabina visi na 4 užeta)

$$F_{\text{st,max}} = \frac{F_{3,\max}}{4} = \frac{12548,8}{4} = 3137,2 \text{ N}$$

Statički faktor sigurnosti

$$S = \frac{F_L}{F_{\text{st,max}}} = \frac{537 d^2}{3137,2} = \frac{537 \cdot 10^2}{3137,2} = 17,1 > 14 \quad \text{zadovoljava}$$

## ZADATAK 28 (5)

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### Brzina dizanja

$$i_{\text{meh}} = \frac{\omega_{\text{EM}}}{v_{\text{diz}}} = \frac{i_{\text{red}}}{R} \quad \Rightarrow \quad v_{\text{diz}} = \frac{\omega_{\text{EM}}}{i_{\text{red}}} R = \frac{142,8}{36} \cdot 0,275 = 1,09$$

$$v_{\text{puz}} = v_{\text{diz}} / 4 = 1,09 / 4 = 0,273$$



# ZADATAK 28 (6)

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## Snaga motora

Najveća obodna sila na pogonskoj užnici javlja se kada je razlika sila najveća

$$P_n = (1,1 \text{ do } 1,2) \frac{F_{\text{pog}} v_{\text{diz}}}{\eta_{\text{meh}}}$$

$$F_{\text{pog}} = F_{3,\text{max}} - F_{2,\text{min}} \quad \eta_{\text{meh}} = \eta_0 \eta_{\text{red}} = 0,98 \cdot 0,65 = 0,637$$

$$F_{2,\text{min}} = G_{\text{ut}} \eta_{\text{ut}} = m_{\text{ut}} g \eta_{\text{ut}} = 925 \cdot 9,81 \cdot 0,98 = 8892,8 \text{ N}$$

$$F_{\text{pog}} = F_{3,\text{max}} - F_{2,\text{min}} = 12548,8 - 8892,8 = 3656 \text{ N}$$

$$P_n = 1,15 \cdot \frac{3656 \cdot 1,09}{0,637} = 7200 \text{ W}$$

Zaključak: motor od 8 kW odgovara

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## ZADATAK 28 (7)

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**Provjera sigurnosti vučnoga pogona za statičko stanje**

$$\mu = \frac{\mu_0}{\sin(\gamma/2)} = \frac{0,09}{\sin(\pi/9)} = 0,263$$

a) Vožnja s punom kabinom prema gore

Radni obuhvatni kut

$$\alpha_{r,1} = \frac{1}{\mu} \ln \left[ \frac{F_{3,\max}}{F_{2,\min}} \right] = \frac{1}{0,263} \ln \left[ \frac{12548,8}{8892,8} \right] = 1,31 \text{ rad} = 75^\circ$$

Sigurnost vučnog pogona

$$S_{v,1} = \frac{e^{\mu\alpha} - 1}{e^{\mu\alpha_{r,s}} - 1} = \frac{e^{0,263 \cdot (8/9)\pi} - 1}{e^{0,263 \cdot 1,31} - 1} = 2,64$$



## ZADATAK 28 (8)

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b) Vožnja s praznom kabinom prema dolje

$$F_{3,\min} = G_{\text{kab}} \eta_{\text{kab}} \eta_0 = 6867 \cdot 0,96 \cdot 0,98 = 6460,5$$

$$F_{2,\max} = G_{\text{ut}} / \eta_{\text{ut}} + G_{\text{už}} = 925 \cdot 9,81 / 0,98 + 546,2 = 9805,66$$

$$\alpha_{r,2} = \frac{1}{\mu} \ln \left[ \frac{F_{2,\max}}{F_{3,\min}} \right] = \frac{1}{0,263} \ln \left[ \frac{9805,66}{6460,47} \right] = 1,586 \text{ rad} = 90,85^\circ$$

$$S_{v,2} = \frac{e^{\mu\alpha} - 1}{e^{\mu\alpha_{r,2}} - 1} = \frac{e^{0,263 \cdot (8/9)\pi} - 1}{e^{0,263 \cdot 1,586} - 1} = 2,096$$



# ZADATAK 28 (9)

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## Dinamička analiza - moment inercije zamašnjaka

$$I_{\text{uk}} = I_{\text{rot}} + I_{\text{tran}} + I_z$$

$$I_{\text{rot}} = 1,15 \cdot (I_{\text{EM}} + I_{\text{S}}) = 1,15 \cdot (0,115 + 0,2) = 0,362$$

$$I_{\text{tra}} = \frac{m_{\text{tra}}}{\eta_{\text{meh}} i_{\text{meh}}^2} = \frac{2161}{0,637 \cdot 130,91^2} = 0,198$$

$$m_{\text{tra}} = \frac{m_{\text{kab}} + m}{\eta_{\text{kab}}} + \frac{m_{\text{už}}}{\eta_0} + m_{\text{ut}} \eta_{\text{ut}} = \left( \frac{700 + 450}{0,96} + \frac{55,68}{0,98} + 925 \cdot 0,98 \right) = 2161$$

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## ZADATAK 28 (10)

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### Dinamička analiza - moment inercije zamašnjaka

$$I_{\text{uk}} = \frac{M_{\text{k}} + M_{\text{st}}}{i_{\text{meh}} a_{\text{k}}} = \frac{128,8 + 43,84}{130,91 \cdot 0,75} = 1,759$$

$$M_{\text{k}} = 2,3 M_{\text{n}} = 2,3 \cdot 56 = 128,8 \text{ Nm}$$

$$M_{\text{st}} = \frac{F_{\text{pog}}}{i_{\text{meh}} \eta_{\text{meh}}} = \frac{3656}{130,91 \cdot 0,637} = 43,84 \text{ Nm}$$

$$I_{\text{z}} = I_{\text{uk}} - (I_{\text{rot}} + I_{\text{tran}}) = 1,759 - (0,362 + 0,198) = 1,2$$



## ZADATAK 28 (11)

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### Vrijeme pokretanja pune kabine prema gore

Jednadžba gibanja pri pokretanju pune kabine prema gore glasi

$$I_{\text{uk}} \varepsilon_{\text{p}} = M_{\text{p}} - M_{\text{st}}$$

$$\varepsilon_{\text{p}} = \frac{M_{\text{p}} - M_{\text{st}}}{I_{\text{uk}}} = \frac{128,8 - 43,84}{1,759} = 48,3 \text{ rad/s}^2$$

$$a_{\text{p}} = \frac{\varepsilon_{\text{p}}}{i_{\text{meh}}} = \frac{48,3}{130,91} = 0,369$$

$$t_{\text{p}} = \frac{v_{\text{diz}}}{a_{\text{p}}} = \frac{1,09}{0,3369} = 2,95$$

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## ZADATAK 28 (12)

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### Kočenje pune kabine prema dolje, bez otpora vođenja

Vrijeme kočenja s elektromotorom od radne brzine do brzine puzanja


$$t_{k,1} = \frac{v_{\text{diz}} - v_{\text{puz}}}{a_k}$$

Jednadžba gibanja

$$I_{\text{uk},k} \varepsilon_k = M_k - M_{\text{st},k} \Rightarrow \varepsilon_k = i_{\text{meh}} a_k = \frac{M_k - M_{\text{st},k}}{I_{\text{uk},k}}$$

$$a_k = \frac{M_k - M_{\text{st},k}}{I_{\text{uk},k} i_{\text{meh}}}$$

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## ZADATAK 28 (13)

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Statičko opterećenje vratila motora

$$M_{st,k} = \frac{F_k}{i_{meh}} \eta_{meh,k} = \frac{2517}{130,91} 0,452 = 8,7$$

$$\eta_{meh,k} = (2 - 1/\eta_{red})(2 - 1/\eta_0) = (2 - 1/0,65)(2 - 1/0,98) = 0,452$$

Sila na obodu pogonske užnice (bez otpora vođenja)

$$F_k = F_3 - F_2 = (m_{kab} + m + m_{už}) g \eta_0 - m_{ut} g$$

$$F_k = [(700 + 450 + 55,68) \cdot 0,98 - 925] \cdot 9,81 = 2517$$

Nakon uvrštavanja slijedi:

$$t_{k,1} = 1,44$$

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# ZADATAK 28 (14)

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## Djelovanje mehaničke kočnice

Pretpostavka:

moment kočenja mehaničke kočnice  $M_{k,meh} = 2M_n = 112 \text{ Nm}$

$$t_{k,meh} = \frac{v_{puz}}{a_{k,meh}} \qquad s_{k,meh} = \frac{v_{puz} t_{k,meh}}{2}$$

$$a_{k,meh} = \frac{M_{k,meh} - M_{st,k}}{I_{uk,k} i_{meh}}$$





# ZADATAK 28 (15)

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## Djelovanje mehaničke kočnice

statičko opterećenje vratila motora

$$M_{st,k} = \frac{F_k}{i_{meh}} \eta_{meh,k} = \frac{2517}{130,91} 0,452 = 8,7$$

$$\eta_{meh,k} = (2 - 1/\eta_{red})(2 - 1/\eta_0) = 0,452$$

$$I_{uk,k} = I_z + I_{rot} + \frac{m_{tra,k}}{i_{meh}^2} \eta_{meh,k} = 1,616$$

Nakon uvrštavanja

$$a_{k,meh} = 0,488$$

$$t_{k,meh} = 0,558$$

$$s_{k,meh} = 0,076$$

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## ZADATAK 28 (16)

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### Sigurnost vučnog pogona pri pokretanju i kočenju

Pokretanje s punom kabinom prema gore

$$F_{\text{pog,p}} = F_{3,\text{p,max}} - F_{2,\text{p,min}} = 13003 - 8551 = 4452$$

$$F_{3,\text{p,max}} = F_{3,\text{max}} + (m_{\text{kab}} + m + m_{\text{už}}) a_p \frac{1}{\eta_0} \quad F_{2,\text{p,min}} = m_{\text{ut}} g \eta_{\text{ut}} - m_{\text{ut}} a_p$$

Obuhvatni kut potreban za ovu obodnu silu je

$$\alpha_p = \frac{1}{\mu} \ln \left[ \frac{F_{3,\text{p,max}}}{F_{2,\text{p,min}}} \right] = \frac{1}{0,263} \ln \left[ \frac{13003}{8551} \right] = 1,593 \text{ rad} = 91,25^\circ$$

sigurnost vučnog prijenosa

$$S_{\text{v,p}} = \frac{e^{\mu\alpha} - 1}{e^{\mu\alpha_p} - 1} = \frac{e^{0,263 \cdot (8/9)\pi} - 1}{e^{0,263 \cdot 1,593} - 1} = 2,08$$

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# ZADATAK 28 (17)

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## Kočenje s punom kabinom prema dolje

$$F_{3,k,\max} = (m_{\text{kab}} + m + m_{\text{už}})(g + a_k)\eta_0$$

$$F_{3,k,\max} = (700 + 450 + 55,68) \cdot (9,81 + 0,568) \cdot 0,98 = 12262$$

$$F_{2,k,\min} = m_{\text{ut}}(g - a_k) = 925 \cdot (9,81 - 0,568) = 8549$$

$$F_k = F_{3,k,\max} - F_{2,k,\min} = 12262 - 8549 = 3713$$

$$\alpha_k = \frac{1}{\mu} \ln \left[ \frac{F_{3,k,\max}}{F_{2,k,\min}} \right] = \frac{1}{0,263} \ln \left[ \frac{12262}{8549} \right] = 1,37 \text{ rad} = 78,54^\circ$$

$$S_{v,k} = \frac{e^{\mu\alpha} - 1}{e^{\mu\alpha_k} - 1} = \frac{e^{0,263 \cdot (8/9)\pi} - 1}{e^{0,263 \cdot 1,37} - 1} = 2,5$$

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# ZADATAK 28 (18)

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## Granično usporenje pri kočenju

$$F_{3,\text{gr}} = (m_{\text{kab}} + m + m_{\text{už}})(g + a_{\text{gr}})\eta_0$$

$$F_{2,\text{gr}} = m_{\text{ut}}(g - a_{\text{gr}})$$

Iz jednakosti sila mora vrijediti:

$$(m_{\text{kab}} + m + m_{\text{už}})(g + a_{\text{gr}})\eta_0 = m_{\text{ut}}(g - a_{\text{gr}})e^{\mu\alpha}$$

$$a_{\text{gr}} = \frac{m_{\text{ut}} e^{\mu\alpha} - (m_{\text{kab}} + m + m_{\text{už}})\eta_0}{m_{\text{ut}} e^{\mu\alpha} + (m_{\text{kab}} + m + m_{\text{už}})\eta_0} g$$

$$a_{\text{gr}} = \frac{925 \cdot e^{0,263 \cdot (8/9)\pi} - (700 + 450 + 55,68) \cdot 0,98}{925 \cdot e^{0,263 \cdot (8/9)\pi} + (700 + 450 + 55,68) \cdot 0,98} \cdot 9,81 = 2,357$$

